# Predicting the functional consequences of amino acid polymorphisms using hierarchical Bayesian models

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which folds spontaneously to a three-dimensional structure.

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- Any nsSNP which disrupts structure is a strong candidate in disease/pharmacogenetic studies

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  - structural data: hydrophobicity, relative B factor, surface accessibility of native amino acid.
  - sequence-based data: conservation of native amino acid in table of multiple sequence alignment.

Lots of recent interest in this (Gunther *et al*, 2003; Stitziel *et al*, 2003; Wang and Moult, 2001; Terp *et al*, 2002; del Sol Mesa *et al*, 2003; Ng and Henikoff, 2002; Chasman and Adams, 2001; Sunyaev *et al*, 2000,2001; Saunders and Baker, 2002)

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- None of these use statistical models: we will build a probabilistic model for protein function.

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- We will train on the Lac repressor and validate on Lysozyme (and vice-versa).

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- Lysozyme molecule from T4 phage:
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  - Amino acids at 143 sites (out of 162) mutated to give a total of 1632 observations.

# **Predictive features used**

Feature	Description
Accessibility	Solvent accessible area of native AA
Relative accessibility	Accessibility relative to maximum accessibility in
	training set
Relative phylogenetic entropy	Normalised phylogenetic entropy of native AA
Neighbourhood rel.	Phylogenetic entropy of structural neighbourhood of
phylogenetic entropy	native AA
Relative <i>B</i> -factor	Normalised B-factor of native AA
Neighbourhood relative	Normalised B-factor of structural neighbourhood of
B-factor	native AA
Unusual AA	Mutant AA is not in phylogenetic profile
Buried charge	Mutant is charged AA at buried site
Turn breaking	Mutant AA occurs at glycine or proline in a turn
Helix breaking	Mutant AA occurs in helical region and involves
	glycine or proline
Conserved	Native AA is at conserved position in phylogenetic
	profile

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$$\eta = \beta_0 + \sum_{k=1}^K \beta_k B_k(\mathbf{x})$$

with *basis functions*  $B_k(\mathbf{x})$  defined as

$$B_k(\mathbf{x}) = \prod_{j=1}^{J_k} \left[ s_{kj} (x_{w_{kj}} - t_{kj}) \right]_+ \quad k = 1, \dots, K$$

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  - Fitted via MCMC

## **Hierarchical BMARS**

For amino acid site i and mutation m assume

$$p(y_{im} = 1 | \boldsymbol{\beta}, \mathbf{x}_{im}, b_i) = \Phi\left(\beta_0 + \sum_{k=1}^K \beta_k B_k(\mathbf{x}_{im}) + b_i\right) = \Phi(\eta_{im} + b_i)$$

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- Probit link for technical reasons—allows us to work out full conditionals for regression parameters and hence we can use gibbs sampling to update these
- Reversible jump MCMC to add, delete or modify a basis function at each iteration.

Fitted values given by

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  - sensitivity: proportion of mutations affecting function correctly classified
  - specificity: proportion of mutations *not* affecting function correctly classified





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- CV misclassification surface is rather flat: taking minimum gives poor performance on test data
- Current analysis uses the smoothest decision boundary leading to acceptable CV misclassification rate



Posterior distribution of the number of basis functions

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#### Relative importance of predictors in the generated sample


#### **Application to mutagenesis data**

The posterior main effect of generic predictor p may be quantified as

$$\hat{E}[\Phi_p(x)] = \frac{1}{L} \sum_{l=1}^{L} \sum_{\substack{k:J_k=1\\w_{1k}=p}}^{L} \beta_k^{(l)} B_k^{(l)}(x)$$

from a posterior sample of size *L*.

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#### Posterior mean interaction between Entropy and Nbhd Rel BF

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- Code available as R package.

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  - But functional biology is hard and expensive
  - Will nsSNPs disrupting function be interesting for genetic epidemiology/pharmacogenetics?