Feedback 17-18

For all questions:

As usually: please, please support your solutions with diagrams!!!.

- Question 17.4:
 - Most solutions of the question started with something like "let's use the classification of isometries" - which is the best strategy here. However, later many students fall into different traps:
 - One should remember there are orientation-preserving isometries and orientation-reversing ones;
 - There are two types of "translations" in \mathbb{H}^2 : the parabolic and the hyperbolic ones!
 - All orientation-preserving isometries in \mathbb{H}^2 have a fixed point in \mathbb{H}^2 or on the absolute. But only the elliptic one have fixed points inside \mathbb{H}^2 . (Fixed points on the boundary do not help to conclude f is identity, as distances are only defined for two points lying inside \mathbb{H}^2).
- Question 17.5:
 - While computing in the hyperboloid model, remember
 - to use the pseudo-scalar product $(\mathbf{u}, \mathbf{v}) = u_1 v_1 + u_2 v_2 u_3 v_3$.
 - to square (u, v) in the numerator of $Q = \frac{(\mathbf{u}, \mathbf{v})^2}{(\mathbf{u}, \mathbf{u})(\mathbf{v}, \mathbf{v})}$
 - Also, remember that when computing in the vector model, it is not necessary to have $\langle a, a \rangle = 1$ (as soon as you do not forget about the denominator in Q). So, you can use the vector which is more convenient for computations (i.e. for example (1, 1, 0) rather than something with $\sqrt{2}$).
 - Remember, if l_1 and l_2 are two intersecting lines forming an angle θ then the composition of reflections in these lines is a rotation by the angle 2θ !

• Question 18.2:

- When working with circles, horocycles of equidistant curves, remember:

they are not straight lines!

In particular, congruence of triangles applies to triangles formed of straight lines, the same holds for any statements about sum of angles.