

## Feedback 17-18

### For all questions:

As usually: please, please support your solutions with **diagrams!!!**.

#### • Question 17.4:

- Most solutions of the question started with something like “let’s use the classification of isometries” - which is the best strategy here. However, later many students fall into different traps:
  - One should remember there are orientation-preserving isometries **and** orientation-reversing ones;
  - There are two types of “translations” in  $\mathbb{H}^2$ : the **parabolic** and the **hyperbolic** ones!
  - All orientation-preserving isometries in  $\mathbb{H}^2$  have a fixed point in  $\mathbb{H}^2$  **or** on the absolute. But only the elliptic one have fixed points inside  $\mathbb{H}^2$ . (Fixed points on the boundary do not help to conclude  $f$  is identity, as distances are only defined for two points lying inside  $\mathbb{H}^2$ ).

#### • Question 17.5:

- While computing in the hyperboloid model, remember
  - to use the pseudo-scalar product  $(\mathbf{u}, \mathbf{v}) = u_1v_1 + u_2v_2 - u_3v_3$ .
  - to square  $(u, v)$  in the numerator of  $Q = \frac{(\mathbf{u}, \mathbf{v})^2}{(\mathbf{u}, \mathbf{u})(\mathbf{v}, \mathbf{v})}$
  - Also, remember that when computing in the vector model, it is not necessary to have  $\langle a, a \rangle = 1$  (as soon as you do not forget about the denominator in  $Q$ ). So, you can use the vector which is more convenient for computations (i.e. for example  $(1, 1, 0)$  rather than something with  $\sqrt{2}$ ).
- Remember, if  $l_1$  and  $l_2$  are two intersecting lines forming an angle  $\theta$  then the composition of reflections in these lines is a rotation by the angle  **$2\theta$** !

#### • Question 18.2:

- When working with circles, horocycles or equidistant curves, remember:

**they are not straight lines!**

In particular, congruence of triangles applies to triangles formed of straight lines, the same holds for any statements about sum of angles.