## ESM 1B, Homework 7

Due Date: 14:00 Thursday, November 5, 2009.

Explain your answers! Problems marked  $(\star)$  are bonus ones.

- **7.1.** Parametrize the curve  $x^2 = y^3$ . Find the normal and tangent components of acceleration with respect to the chosen parameter. Find the curvature of this curve as a function of (x, y).
- **7.2.** (a) Find the arc-length parameter on the parabola  $x = y^2$ , setting the initial point (i.e. where s = 0) to be (0,0).
  - (b) Compute the length of the curve  $y = x^3$ ,  $-1 \le x \le 1$ .
- **7.3.** Give a coordinate equation of the tangent plane to the surface

$$x = \sin u$$
,  $y = \cos v$ ,  $z = u + v$ 

at point  $(u_0, v_0)$ .

**7.4.** Evaluate the integral

$$\int_0^1 \left[ \vec{a} \left( \frac{d\vec{a}}{dt} \cdot \vec{b} + \vec{a} \cdot \frac{d\vec{b}}{dt} \right) + \frac{d\vec{a}}{dt} (\vec{a} \cdot \vec{b}) \right] dt$$

- **7.5.** (a) Write an equation of the tangent line to the curve x = y on the surface  $x^2 y^2 + z = 2$  at the point (1, 1, 2);
  - (b) Write the coordinate equation of the plane tangent to the surface

$$xy + \cos z = 0$$

at the point  $(1/2, -\sqrt{3}, \pi/6)$ .

- **7.6.** (a) Compute the surface area of the paraboloid  $z=x^2+y^2,\,0\leq z\leq 1;$ 
  - (\*) Compute the area of the part of the surface  $x^2 + y^2 = Rx$  contained inside the sphere  $x^2 + y^2 + z^2 = R^2$ .