## ESM 1B, Homework 7

Due Date: 14:00 Thursday, November 5, 2009.

Explain your answers! Problems marked $(\star)$ are bonus ones.
7.1. Parametrize the curve $x^{2}=y^{3}$. Find the normal and tangent components of acceleration with respect to the chosen parameter. Find the curvature of this curve as a function of $(x, y)$.
7.2. (a) Find the arc-length parameter on the parabola $x=y^{2}$, setting the initial point (i.e. where $s=0)$ to be $(0,0)$.
(b) Compute the length of the curve $y=x^{3},-1 \leq x \leq 1$.
7.3. Give a coordinate equation of the tangent plane to the surface

$$
x=\sin u, \quad y=\cos v, \quad z=u+v
$$

at point $\left(u_{0}, v_{0}\right)$.
7.4. Evaluate the integral

$$
\int_{0}^{1}\left[\vec{a}\left(\frac{d \vec{a}}{d t} \cdot \vec{b}+\vec{a} \cdot \frac{d \vec{b}}{d t}\right)+\frac{d \vec{a}}{d t}(\vec{a} \cdot \vec{b})\right] d t
$$

7.5. (a) Write an equation of the tangent line to the curve $x=y$ on the surface $x^{2}-y^{2}+z=2$ at the point $(1,1,2)$;
(b) Write the coordinate equation of the plane tangent to the surface

$$
x y+\cos z=0
$$

at the point $(1 / 2,-\sqrt{3}, \pi / 6)$.
7.6. (a) Compute the surface area of the paraboloid $z=x^{2}+y^{2}, 0 \leq z \leq 1$;
(*) Compute the area of the part of the surface $x^{2}+y^{2}=R x$ contained inside the sphere $x^{2}+y^{2}+z^{2}=R^{2}$.

